

$$\begin{cases} x - 5y + 3z = 9 & (1) \\ 2x - y + 4z = 6 & (2) \\ 3x - 2y + z = 2 & (3) \end{cases}$$

Élimination de z:

$$\begin{array}{l|l} (1) & x - 5y + 3z = 9 \\ -3 \cdot (3) & -9x + 6y - 3z = -6 \\ \hline \Sigma & -8x + y \quad \quad \quad = 3 \quad (4) \end{array}$$

$$\begin{array}{l|l} (2) & 2x - y + 4z = 6 \\ -4 \cdot (3) & -12x + 8y - 4z = -8 \\ \hline \Sigma & -10x + 7y \quad \quad \quad = -2 \quad (5) \end{array}$$

$$\begin{array}{l|l} -7 \cdot (4) & 56x - 7y = -21 \\ (5) & -10x + 7y = -2 \\ \hline \Sigma & 46x \quad \quad \quad = -23 \quad \text{donc } x = -\frac{23}{46} = -\frac{1}{2} \end{array}$$

Substituer x dans (4)

$$-8 \cdot \left(-\frac{1}{2}\right) + y = 3 \quad \text{donc } y = -1$$

Substituer x et y dans (1)

$$-\frac{1}{2} - 5(-1) + 3z = 9 \quad \text{donc } z = \frac{3}{2}$$

Solution: $x = -\frac{1}{2}$, $y = -1$, $z = \frac{3}{2}$

Preuve: dans (2), par exemple

$$2 \cdot \left(-\frac{1}{2}\right) - (-1) + 4\left(\frac{3}{2}\right) = -1 + 1 + 6 = 6 \quad \checkmark$$